

# Type-Driven *Design* of Communicating Systems using Idris

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It is always good to start with a joke. . .

Jan "Knock Knock"

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Audience "Who's there?"

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Jan "Amosquito! dummy!"  
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Knock-Knock is a 'well known' joke.

- Doesn't follow the **known specification**.
- Messages are in the wrong order and format.
- Unknown participants  $\implies$  unknown channels.
- Messages might arrive late. . .

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Jan "Knock Knock"  
Audience "Who's there?"  
Jan "Amosquito! dummy!"  
Audience "Amosquito! dummy! who?"  
Ken "Amos"  
Eve "Not this stupid joke again!"

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# Knock Knock: Specifications

## Informal Narration.

- 1  $A \rightarrow B$  : "Knock, Knock"
- 2  $B \rightarrow A$  : "Who's there?"
- 3  $A \rightarrow B$  : *msg*
- 4  $B \rightarrow A$  : *msg* ++ " who?"
- 5  $A \rightarrow B$  : *msg* ++ *resp*

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## Global Type (MPST)

- 1  $A \rightarrow B$  :  $k\langle\text{String}\rangle$ .
- 2  $B \rightarrow A$  :  $k\langle\text{String}\rangle$ .
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## Session Types are great but not *perfect*

- Hard to reason on messages.
- Hard to reason on channel management.

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- Establish:  $K_{A,AS}$
- $Alice \rightarrow AS : ID(A)$
- AS generates
  - ticket with TTL:  $\mathcal{T}_{ttl} \leftarrow \{ID(A) \parallel K_{A,TGS}\}_{K_{AS,TGS}}$
  - Session Key  $K_{A,TGS}$
- $AS \rightarrow Alice : \{K_{A,TGS} \parallel \mathcal{T}_{ttl}\}_{K_{A,AS}}$

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## 2 Request Ticket from TGS to Talk to Bob

- Establish:  $K_{A,TGS}$  & Alice generates: Timestamp  $t$ .
- $A \rightarrow TGS : \mathcal{T}_{ttl} \parallel ID(B) \parallel \{t\}_{K_{A,TGS}}$
- TGS generates Session Key  $K_{A,B}$  and obtains  $K_{B,TGS}$ .
- $TGS \rightarrow A : \{ID(B) \parallel K_{A,B}\}_{K_{A,TGS}} \parallel \{ID(A) \parallel K_{A,B}\}_{K_{B,TGS}}$

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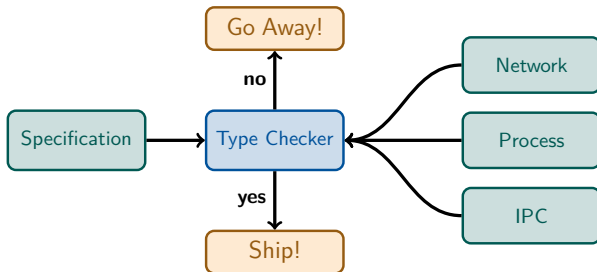
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## 3 Ask Bob To Talk

- $A \rightarrow B : \{ID(A) \parallel K_{A,B}\}_{K_{B,TGS}} \parallel \{t\}_{K_{A,B}}$
- $B \rightarrow A : \{t + 1\}_{K_{A,B}}$

# Type-Driven Verification of Communicating Systems



System to describe, reason, and build Communicating Systems:

- Inspired by [Session Types](#).
- Leverage [Dependent Types](#) & [Algebraic Effects](#) as presented in Idris.
  - <http://www.idris-lang.org>



# Sessions Modelling Language

- Describing Sessions i.e. Global Types
  - EDSL encoded as a Data Type.
  - Automatic trace generation.
- Using Idris control structures
  - Do Notation—Linearity
  - Case Splits—Branches
  - Recursion—Iteration
- Fine-grained Channel Management
  - Creation, Use, Destruction.
  - Cannot use a disconnected channel.
- Actor Management
  - When Actors can be used.
- Reason on Description
  - 'Resource'-Dependent State Changes
  - Predicates & Idris' Proof Search

```

data Session : (ty : Type)
              -> (old : Context)
              -> (new : ty -> Context)
              -> Type
  
```

```

where
  Activate...    Call...
  Deactivate...  Rec...
  NewChannel...  Done...
  RmChannel...   (>>=)...
  Startup...     Pure...
  Teardown...
  Send...
  
```

# TCP 'Handshake': Naïve

1  $A \rightarrow B : (\text{Syn}, x)$

2  $B \rightarrow A : (\text{SynAck}, y, x + 1)$

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- 1  $A \rightarrow B : k\langle \text{TCPMsg}, \text{Nat} \rangle .$
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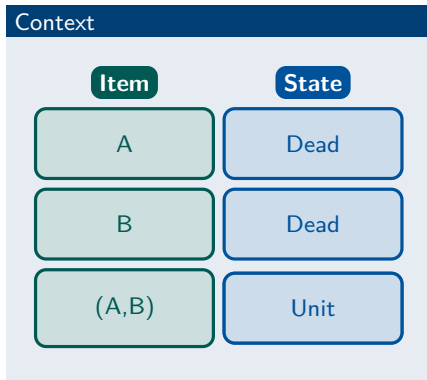
`Handshake : Session [A,B] [(A,B)] ()`

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Handshake = do
  activateAll
  chan <- channel A B
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  send chan B A (TCPMsg, Nat, Nat)
  send chan A B (TCPMsg, Nat, Nat)
  shutdown chan A
  deactivateAll
end
```

# TCP 'Handshake': Naïve—The 'Context'

```
Handshake : Session [A,B]
            [(A,B)]
            () ●
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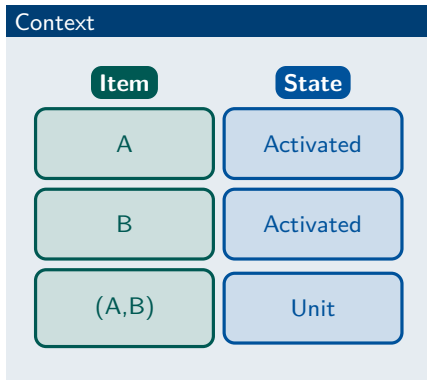
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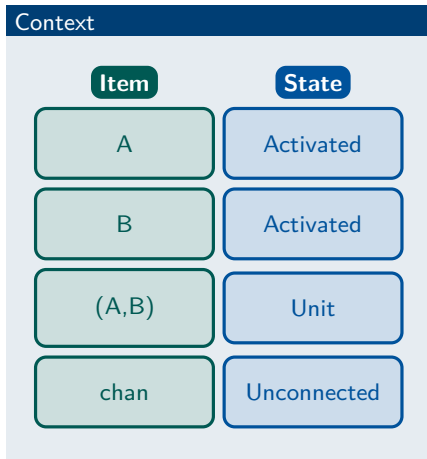
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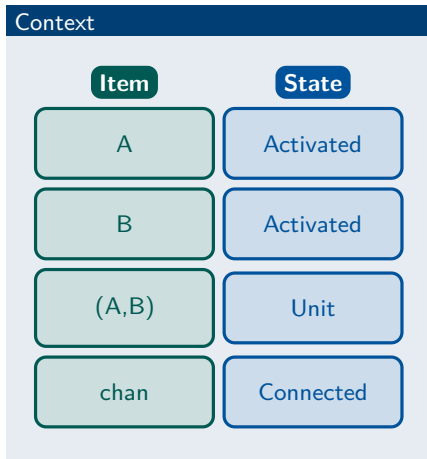
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```





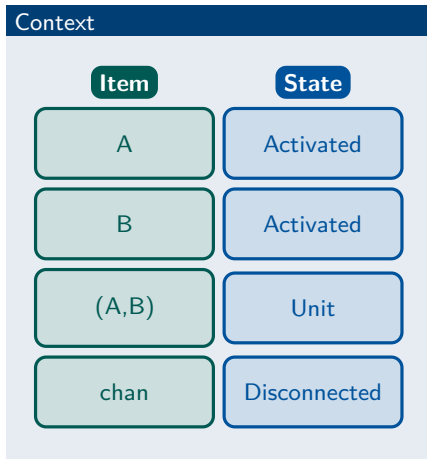
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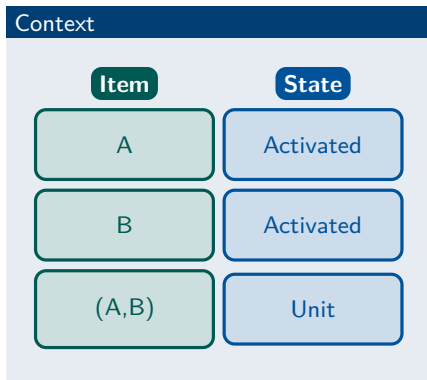
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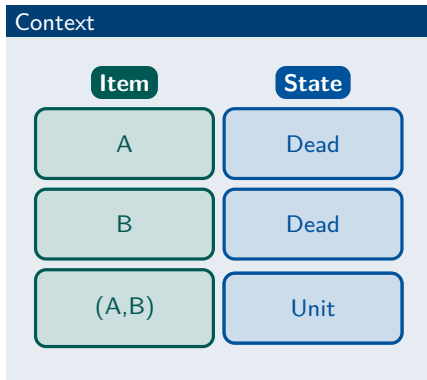
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  send chan A B (TCPMsg, Nat, Nat)
  shutdown chan A
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end ●

```



# TCP 'Handshake': Naïve

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- 1  $A \rightarrow B : k\langle \text{TCPMsg}, \text{Nat} \rangle .$
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`Handshake : Session [A,B] [(A,B)] ()`

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Handshake = do
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  startup chan
  send chan A B (TCPMsg, Nat)
  send chan B A (TCPMsg, Nat, Nat)
  send chan A B (TCPMsg, Nat, Nat)
  shutdown chan A
  deactivateAll
end
```

# TCP 'Handshake': Improved

- 1  $A \rightarrow B : (\text{Syn}, x)$
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- 1  $A \rightarrow B : k \langle \text{TCPMsg}, \text{Nat} \rangle .$
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- 3  $A \rightarrow B : k \langle \text{TCPMsg}, \text{Nat}, \text{Nat} \rangle . \text{end}$

`Handshake` : `Session [A,B] [(A,B)] ()`

`Handshake` = do

`activateAll`

`chan` <- `channel A B`

`startup chan`

`(_,x)` <- `send chan A B (TCPMsg, Nat)`

`(_,y,_)` <- `send chan B A (TCPMsg, Nat, (x' ** x' = S x))`

`send chan A B (TCPMsg, (y' ** y' = S y), (x' ** x' = S x))`

`shutdown chan A`

`deactivateAll`

`end`

# TCP 'Handshake': Better

- 1  $A \rightarrow B : (\text{Syn}, x)$
- 2  $B \rightarrow A : (\text{SynAck}, y, x + 1)$
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- 3  $A \rightarrow B : k \langle \text{TCPMsg}, \text{Nat}, \text{Nat} \rangle . \text{end}$

`Handshake` : `Session [A,B] [(A,B)] ()`

`Handshake` = do

`activateAll`

`chan` <- `channel A B`

`startup chan`

`(_, x)` <- `send chan A B (TCPMsg, Nat)`

`(_, y, _)` <- `send chan B A (TCPMsg, Nat, Next x)`

`send chan A B (TCPMsg, Next y, Next x)`

`shutdown chan A`

`deactivateAll`

`end`

# TCP 'Handshake': Best

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`Handshake` : `Session [A,B] [(A,B)] ()`

`Handshake` = do

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`chan` <- `channel A B`

`startup chan`

`(_,x)` <- `send chan A B (TCPMsg SYN, Nat)`

`(_,y,_)` <- `send chan B A (TCPMsg SYNACK, Nat, Next x)`

`send chan A B (TCPMsg ACK, Next y, Next x)`

`shutdown chan A`

`deactivateAll`

`end`

# Implementing Sessions: Sample Language Expressions

```

Activate : (a      : Actor)
  -> (idx : InContextP ACTOR (ActorHasState a DEAD) item ctxt)
  -> Session ()
      ctxt
      (\res => updateStateP ACTIVE ctxt idx)

```

```

Send : (c      : VarChannel chan)
  -> (s      : Actor)
  -> (r      : Actor)
  -> (mTy    : Type)
  -> (ok_s   : InContextP ACTOR (ActorHasState s ACTIVE) iS ctxt)
  -> (ok_r   : InContextP ACTOR (ActorHasState r ACTIVE) iR ctxt)
  -> (ok_c   : InContextP CHANNEL
      (ChannelHasState chan c CONNECTED) iC ctxt)
  -> (vsend  : ValidSend s r c mTy rTy iC)
  -> Session rTy ctxt (\res => ctxt)

```



# Implementing Sessions: Proofs and Predicates

## Predicated Index

```

data InContextP : (ty : Ty)      -> (p : Item ty -> Type)
                  -> (x  : Item ty) -> (c : Context) -> Type

  where
    HereP  : p x -> InContextP ty p x (x :: rest)
    ThereP : InContextP ty p x rest
            -> InContextP ty p x (notitem :: rest)
  
```

## Example Predicate

```

data ActorHasState : (actor : Actor )
                    -> (value : AState)
                    -> (item  : Item ACTOR)
                    -> Type

  where
    AState : ActorHasState a
            value
            (MkItem label (ReprActor a) value)
  
```

# Simplified Kerberos—Sans Crypto

```
Kerberos' : Session () [A,B,T,K] [(A,B), (A,T), (A,K)]
```

```
Kerberos' = do
```

```
  activateSet [A,K]
```

```
  kak <- channel A K  -- Contact Authentication Service
```

```
  startup kak
```

```
  aliceID <- send kak A K String
```

```
  (_, ticket) <- send kak K A (Literal String aliceID, String)
```

```
  shutdown kak A
```

```
  activate T
```

```
  kat <- channel A T  -- Request Ticket
```

```
  startup kat
```

```
  (_, bobID, t) <- send kat A T (Literal String ticket, String, Nat)
```

```
  (_, y) <- send kat T A ( (Literal String bobID, String)
                        , (Literal String aliceID, String))
```

```
  shutdown kat A
```

# Simplified Kerberos—Sans Crypto—cont. . .

```
activate B    -- Talk to Bob
kab <- channel A B
startup kab
send kab A B ( Literal (Literal String aliceID, String) y
              , Literal Nat t)
send kab B A (Next t)
shutdown kab A

deactivateAll
end
```

# Authentication Protocol: Simplified Kerberos

Establish a secure connection using a *Trusted Third Party*.

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- Establish:  $K_{A,TGS}$  & Alice generates: Timestamp  $t$ .
- $A \rightarrow TGS : \mathcal{T}_{ttl} \parallel ID(B) \parallel \{t\}_{K_{A,TGS}}$
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## 3 Ask Bob To Talk

- $A \rightarrow B : \{ID(A) \parallel K_{A,B}\}_{K_{B,TGS}} \parallel \{t\}_{K_{A,B}}$
- $B \rightarrow A : \{t + 1\}_{K_{A,B}}$

# RFC 347 & 862

## RFC 347 &amp; 862

1  $A \rightarrow B : x$

2  $B \rightarrow A : x$

```

μt. A → B : k{
  echo ⇒ A → B : k⟨String⟩
    .B → A : k⟨String⟩
    .t
  quit ⇒ end}

```

## RFC 347 &amp; 862

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      . t
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```

```

Echo : Session ()
      [Client, Server]
      [(Client,Server)]

Echo = do
      activateAll

      net <- channel Client Server
      startup net
      call $ doEcho net
      shutdown net Server

      deactivateAll
      end

```

# RFC 347 & 862: Looping

```
doEcho : (chan : CHAN Client Server)
  -> SubSession () (CommonContextCS chan)
doEcho net = do
  case !(send net Client Server (Maybe String)) of
    Just m => do
      send net Server Client $ Literal String m
      rec $ doEcho net
    Nothing => done
```



# RFC 347 & 862: Looping

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    Just m => do
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      rec $ doEcho net
    Nothing => done
```

```
Rec : Inf (Session a ctxt ctxt') -> Session a ctxt ctxt'
```

```
Call : (sub : Session a ctxt' (const ctxt'))
       -> (prf : SubContext ctxt' ctxt)
       -> Session a ctxt ctxt
```

# Codified Designs

## 'Real' Protocols

- RFC 347 Echo
- RFC 862 Echo
- RFC 864 CharGen
- RFC 867 DayTime
- RFC 868 Time

## Not So Real Protocols

- Hello World.
- Greeter Program.
- String Length
- Natural Number Calculator
- TCP Handshake

# Further Work

Short project, with much long term potential. . .

## ■ Communication Contexts

- *Almost* link specifications and implementations using algebraic effects.
- Constructing Network, IPC, & Process implementations.
- Context Agnostic Contexts?

## ■ More 'Real' & Complex Examples

- Different Protocols, Workflows, & Processes
- Multi-party Communications
- TCP, TLS, SPEKE, TFTP, PGP. . . .

## ■ Look beyond the interaction.

- Formal verification of the Specification.
- Applied-II, CSP. . .

# Summary

## Dependent Types helps Session Types

*Session Types, I think this is the beginning of a beautiful friendship.*

- Implement *most* of Session Types.
- Reason on Messages & Channel Management.
- Better environment to reason about protocols.

## Lots of interesting Future work

*To Implementations, and Beyond!*

- Linking specifications with implementations using algebraic effects.
- Guarantees over 'non-functional' properties *a la* ProVerif.